# Structures, Stabilities, and Bonding in $\mathrm{CBe}_{2}, \mathrm{C}_{2} \mathrm{Be}$, and $\mathrm{C}_{2} \mathrm{Be}_{2}$ 

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#### Abstract

The structures and energies of the binary beryllium compounds $\mathrm{CBe}_{2}, \mathrm{C}_{2} \mathrm{Be}$, and $\mathrm{C}_{2} \mathrm{Be}_{2}$ in their energetically lowest singlet and triplet states have been investigated by means of ab initio quantum chemical methods, employing second order Moller-Plesset (MP2) perturbation theory and, for the triatomic molecules, CASSCF techniques. Nonlinear geometries are predicted to be the global minima for $\mathrm{CBe}_{2}\left({ }^{1} \mathrm{~A}_{1}\right)$ and $\mathrm{C}_{2} \mathrm{Be}\left({ }^{1} \mathrm{~A}_{1}\right)$ by both methods, MP2/6-31G*//6-31G* and CASSCF using a $D Z+P$ basis set and an active space of eight electrons in nine orbitals. For $C_{2} \mathrm{Be}_{2}$, the $\mathrm{MP} 2 / 6-31 \mathrm{G} * / / 6-31 \mathrm{G}^{*}$ results favor a linear triplet isomer $\left({ }^{3} \Sigma_{u}{ }^{+}\right)$by more than $80 \mathrm{kcal} / \mathrm{mol}$ relative to the next low-lying structure (a cyclic form, ${ }^{1} \mathrm{~A}_{1}$ ). The results of one electron density analysis indicate that charge transfer from Be to C is responsible for the stabilities of the nonlinear isomers and that there is little covalent CBe bonding in the singlet nonlinear minima of $\mathrm{CBe}_{2}$ and of $\mathrm{C}_{2} \mathrm{Be}$.


## I. Introduction

The structures of organic molecules containing electropositive elements often are influenced crucially by coulomb forces; as a consequence bridged or nonclassical structures occur frequently. This is exemplified by the unusual geometries of organolithium compounds, which seldom favor the typical structures of covalent compounds. ${ }^{1}$ Moreover, boron compounds, although usually considered to be covalent, also frequently prefer bridged structures and sometimes very unusual geometries. ${ }^{2}$ Less is known about beryllium compounds, but available results indicate that bridged structures also are common. ${ }^{3}$ A recent theoretical investigation of $\mathrm{CBe}_{2}$ in the crystal state ${ }^{4}$ indicated a high degree of ionicity but also an important contribution of covalent bonding. Analysis of the computed wave function may reveal the nature of the bonding. Since Mulliken population analysis has been shown to be unreliable for compounds with electropositive elements, ${ }^{5}$ we prefer to employ an analysis of the one electron density which has been demonstrated to be highly useful for the interpretation of the nature of bonding in molecules. ${ }^{6}$ This paper reports results of an $a b$ initio investigation of the structures, stabilities, and bonding of $\mathrm{CBe}_{2}, \mathrm{C}_{2} \mathrm{Be}$, and $\mathrm{C}_{2} \mathrm{Be}_{2}$.

## II. Computational Details

Theoretical investigations have been performed by using a modified Gaussian 76 program, ${ }^{7}$ which includes the Davidon-Fletcher-Powell multiparameter search ${ }^{8}$ with analytically evaluted forces ${ }^{9}$ for the 3-21G basis set. ${ }^{10}$ Stationary points on the potential energy hypersurface at $3-21 \mathrm{G}$ have been checked by diagonalization of the force-constant matrix, and the optimized geometries reported here have only positive eigenvalues in the Hessian matrix. Further geometry optimization has been carried out with the polarized $6.31 \mathrm{G}^{*}$ basis with parabolic search. Correlation energy has been estimated for the single-point calculations by MollerPlesset perturbation theory terminated at second order ${ }^{11}$ in the frozencore approximation. This level of theory is denoted MP2/6-31G*//631G*. For the calculation of the triplet states we used the unrestricted Hartree-Fock (UHF) method. ${ }^{12}$ The optimizations of the linear triatomic triplets have frequently been marked by technical problems such as jumping among several states and high spin contamination. The results presented here have been obtained by using damping for the initial SCF iterations and choosing the lowest energy isomer irrespective of the degree of spin contamination.

CASSCF calculations ${ }^{13}$ have been performed for all triatomic singlets and triplets by using analytical gradients for the geometry optimizations. ${ }^{14}$ For carbon, the ( 10 s 6 pld ) basis set contracted to ( 5 s 4 pld ) developed by Huzinaga ${ }^{15}$ and Dunning ${ }^{16}$ and for beryllium, a (12s5pld) basis set contracted to (7s3pld) were employed; ${ }^{17}$ both are of double- $\zeta$ plus polarization ( $D Z+P$ ) quality. For the active space, eight electrons in nine valence orbitals have been chosen, with the three lowest lying

[^0]doubly occupied MOs for $\mathrm{CBe}_{2}$ (four in case of $\mathrm{C}_{2} \mathrm{Be}$ ) taken as frozen core.

## III. Results and Discussion

Our computed total and relative energies of the optimized geometries are listed in Table I, and the geometrical details are shown in Table II. Properties of the one-electron density distribution $\zeta(r)^{6.18}$ of some selected CBe compounds are summarized in Table III.
$\mathrm{CBe}_{2}$. Only one singlet form, the nonlinear species 1 S , has been found to be a minimum on the $\mathrm{CBe}_{2}$ potential energy hypersurface. However, the energies of the three triplets, $1 \mathrm{~T}, 2 \mathrm{~T}$, and 3 T , relative to 1 S , vary considerably with the level of theory employed. As is generally the case, (UHF) SCF data artifically favor triplets over singlets. Due to the high spin contamination, the SCF results show an unrealistic perference for the linear triplet isomers. The inclusion of correlation energy at the MP2 level leads to drastic
(1) Schleyer, P. v. R, Pure Appl. Chem. 1983, 55, 355 and references therein.
(2) (a) Frenking, G.; Schaefer, H. F., III. Chem. Phys. Lett 1984, $109,521$. (b) Budzelaar, P. H. M.; Schleyer, P. v. R.; Krogh-Jespersen, K. Angew. Chem., Inl. Ed. Engl. 1984, 23, 825.
(3) (a) Dill, J. D.; Schleyer, P. v. R.; Binkley, J. S.; Pople, J. A. J. Am. Chem. Soc. 1977, 99, 6159. (b) Dewar, M. J. S.; Rzepa, H. S. J. Am. Chem. Soc. 1978, 100, 777. (c) Jemmis, E.; Alexandratos, S.; Schleyer, P. v. R.; Streitwieser, A.; Schaefer, H. F. J. Am. Chem. Soc. 1978, 100, 5695. (d) Marynick, D. S. J. Am. Chem. Soc. 1981, 103, 1328. (e) Cremer, D. "General and Theoretical Aspects of the Peroxide Group"; In The Chemistry of Functional Groups, Peroxides; Patai, S., Ed.; Wiley: New York, 1983; p 1.
(4) Herzig, P.; Redinger, J. J. Chem. Phys. 1985, 82, 372.
(5) Bachrach, S. M.; Streitweiser, A.; Jr. J. Am. Chem. Soc. 1984, 106, 2283.
(6) (a) Bader, R. F. W.; Slee, T. S.; Cremer, D.; Kraka, E. J. Am. Chem. Soc. 1983, 105, 5061. (b) Cremer, D.; Kraka, E.; Slee, T. S.; Bader, R. F. W.; Lau, C. D.H.; Nguyen Dang, T. T. MacDougall, P. J. J. Am. Chem. Soc. 1983, $105,5069$.
(7) Binkley, J. S.; Whiteside, R. A.; Hariharan, P. C.; Seeger, R.; Pople, J. A.; Hehre, W. J.; Newton, M. D. QCPE 368.
(8) (a) Fletcher, R.; Powell, M. D. Comput. J. 1963, 6, 163. (b) Davidon, W. C. Comput. J. 1968, 10, 406. (c) Poppinger, D. Chem. Phys. Lett. 1975, 34, 1975.
(9) Schlegel, H. B.; Wolfe, S.; Bernardi, F. J. Chem. Phys. 1975, 63, 3632; incorporated in Gaussian 76 by H. B. Schlegel and J. Chandrasekhar.
(10) Binkley, J. S.; Pople, J. A.; Hehre, W. J. J. Am. Chem. Soc. 1980, 102, 939.
(11) (a) Moller, C.; Plesset, M. S. Phys. Rev. 1934, 46, 618. (b) Binkley, J. S.; Pople, J. A. Int. J. Quantum Chem. 1975, 9S, 229.
(12) Pople, J. A.; Nesbet, R. K. J. Chem. Phys. 1954, 22, 571.
(13) Siegbahn, P. E. M.; Almlöf, J.; Heiberg, A.; Roos, B. O. J. Chem. Phys. 1981, 74, 2384.
(14) Helgaker, T.; Almlöf, J. to be published.
(15) Huzinaga, S. J. Chem. Phys. 1965, 42, 1293.
(16) Dunning, T. H. J. Chem. Phys. 1971, 55, 716
(17) Dykstra, C.; Schaefer, H. F. III; Meyer, W. J. Chem. Phys. 1977, 65, 5141.
(18) (a) Cremer, D.; Kraka, E. Angew. Chem., Int. Ed. Engl. 1984, 23, 627. (b) Cremer, D.; Kraka, E. Croat. Chem. Acta 1984, 57, 1265. (c) Cremer, D.; Kraka, E. J. Am. Chem. Soc. 1985, 107, 3800, 3811

Table I.

| molec. | symm. | state | 3-21G/3-21G |  |  | 6-31G*/6-31G* |  |  | $\begin{gathered} \mathrm{MP} 2 / 6-31 \mathrm{G}^{*} / / \\ 6-31 \mathrm{G}^{*} \end{gathered}$ |  | CASSCF |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | $E_{\text {tot }}$ | $\left\langle S^{2}\right\rangle$ | $\mathrm{E}_{\text {rel }}$ | $E_{\text {tot }}$ | ( $\mathbf{S}^{2}$ ) | $E_{\text {rel }}$ | $E_{\text {tot }}$ | $E_{\text {rel }}$ | $E_{\text {tot }}$ | $E_{\text {rel }}$ |
| (a) Calculated Total (au) and Relative ( $\mathrm{kcal} / \mathrm{mol}$ ) Energies of $\mathrm{CBe}_{2}$ Forms |  |  |  |  |  |  |  |  |  |  |  |  |
| 15 | $C_{2 v}$ | ${ }^{1} \mathrm{~A}_{1}$ | -66.5083 |  | 68.3 | -66.8843 |  | 65.6 | -67.1113 | 0.0 | -67.0454 | 0.0 |
| 1 T | $C_{2}$ | ${ }^{3} \mathrm{~B}_{1}$ | -66.5413 | 2.13 | 47.6 | -66.9171 | 2.21 | 45.0 | -67.1793 | 20.1 | -67.0176 | 17.4 |
| 2 T | $D_{\text {wh }}$ | ${ }^{3} \Sigma_{u}{ }^{+}$ | -66.6172 | 3.01 | 0.0 | -66.9888 | 3.01 | 0.0 | -67.1000 | 7.1 | -67.0126 | 20.6 |
| 3 T | $C_{\alpha_{v}}$ | ${ }^{3} \pi$ | -66.5363 | 3.07 | 50.8 | -66.9024 | 3.12 | 54.2 | -67.0057 | 66.3 | -66.9578 | 54.9 |
| (b) Calculated Total (au) and Relative ( $\mathrm{kcal} / \mathrm{mol}$ ) Energies of $\mathrm{C}_{2} \mathrm{Be}$ Fotms |  |  |  |  |  |  |  |  |  |  |  |  |
| 4S | $C_{2 v}$ | ${ }^{1} \mathrm{~A}_{1}$ | -89.6522 |  | 25.9 | -90.1770 |  | 9.2 | -90.4666 | 0.0 | -90.3329 | 0.0 |
| 4 T | $C_{2 c}$ | ${ }^{3} \mathrm{~B}_{2}$ | -89.5979 | 2.01 | 60.0 | -90.1129 | 2.01 | 49.4 | -90.3574 | 68.5 | -90.2109 | 76.5 |
| 5 S | $C_{\alpha_{i t}}$ | ${ }^{1} \Sigma^{+}$ | -89.6374 |  | 35.2 | -90.1392 |  | 32.9 | -90.4094 | 35.9 | -90.3249 | 5.0 |
| 5 T | $C_{\text {w }}$ | ${ }^{3} \Sigma^{+}$ | -89.6935 | 2.55 | 0.0 | -90.1917 | 2.50 | 0.0 | -90.3919 | 46.9 | -90.3219 | 6.9 |
| (c) Calculated Total (au) and Relative (kcal/mol) Energies of $\mathrm{C}_{2} \mathrm{Be}_{2}$ Forms |  |  |  |  |  |  |  |  |  |  |  |  |
| 6S | $C_{s}$ | ${ }^{\prime} \mathrm{A}_{1}$ | -104.2249 |  | 55.2 | -104.8272 |  | 42.4 | -105.0345 | 83.8 |  |  |
| 7 S | $D_{\text {ah }}$ | ${ }^{1} \Sigma^{3} \mathrm{~g}_{+}+$ | -104.0797 |  | 146.3 | -104.6590 |  | 148.0 | -104.8587 | 194.1 |  |  |
| 7 T | $D_{\text {® } h}$ | ${ }^{3} \Sigma^{3}{ }^{4}+$ | -104.3129 | 2.01 | 0.0 100.3 | -104.8948 | 2.00 | 0.0 | -105.1680 | 0.0 |  |  |
| 8 T | $C_{2 v}$ | ${ }^{3} \mathrm{~B}_{1}$ | -104.1531 | 2.11 | 100.3 | -104.7471 | 2.11 | 92.7 | -104.9014 | 167.3 |  |  |
| 9 S | $D_{2 h}$ | ${ }^{1} \mathrm{~A}_{\mathrm{g}}$ | -104.1797 |  | 83.6 | -104.7913 |  | 64.9 | -104.9956 | 108.2 |  |  |
| 9 T | $C_{2 v}$ | ${ }^{3} \mathrm{~A}_{2}$ | -104.1252 | 2.22 | 117.8 | -104.7066 | 2.17 | 118.1 | -104.9789 | 118.7 |  |  |

Table II. Optimized Geometries ${ }^{a}$

${ }^{a}$ CASSCF data are given in italics, 3-21G data in parentheses; all other values are at 6 -31G* level. Distances are given in $\AA$, angles in degrees.
changes in relative stabilities which further demonstrate the unreliability of the SCF results. Hqwever, CASSCF and MP2/6$31 \mathrm{G}^{*}$ energy values agree that the nonlinear singlet isomer 1 S is the global $\mathrm{CBe}_{2}$ minimum. This contrasts sharply with $\mathrm{A}_{2} \mathrm{~B}$ molecules with $10-16$ valence electrons, where linear forms are expected to be the most stable isomers by Walsh's rules. ${ }^{19}$

The theoretical interatomic distances for 1 S (Table II), 1.556 (6-31 $G^{*}$ ) and $1.607 \AA$ (CASSCF) for C-Be, are substantially less than the standard value for a carbon-beryllium single bond ( $1.69 \AA$ ) ${ }^{\text {3a }}$ The computed $\mathrm{Be}-\mathrm{Be}$ distances correspond closely

[^1]to the standard value for a single bond ( $2.10 \AA$ ). ${ }^{3 a}$ Assuming that three-membered rings have bent bonds (like cyclopropane), the internuclear distances should be smaller than in the corresponding acyclic reference compounds. On this basis, the geometry of $\mathrm{CBe}_{2}$ (IS) points to enhanced $\mathrm{C}-\mathrm{B}$ bonding but decreased $\mathrm{Be}-\mathrm{Be}$ bonding. This suggestion is supported by an analysis of the one-electron density distribution $\zeta(r)$ of 1 S. As shown in Figure la, there are two paths of maximum electron density (bond paths $)^{6.18}$ which connect C with the Be atoms. The shift in the position of the bond critical points ${ }^{20}$ (dots in Figure 1) toward the Be nuclei indicates the large polarity of the CBe bonds. ${ }^{21}$ There is no $\mathrm{Be}, \mathrm{Be}$ bond path, although the Laplace concentration $\nabla^{2} \zeta(r)^{22}$ depicted in the form of contour line diagrams in Figure 1 clearly reveals that there is an attractive $\mathrm{Be}, \mathrm{Be}$ interaction leading to some electron concentration in the $\mathrm{Be}, \mathrm{Be}$ internuclear region (dashed contour lines in Figure 1a). This, however, is far less pronounced than the charge concentration in the CBe region; the attractive $\mathrm{Be}, \mathrm{Be}$ interactions evidently are not sufficient for covalent bonding. iS possesses an acyclic structure ${ }^{23}$ contrary to expectations resulting from geometrical data.

Characteristically, all the calculated $\nabla^{2} \zeta(r)$ distributions in Figure 1 show large areas of electron charge depletion surrounding the Be nuclei and the innermost shell with $\nabla^{2} \zeta(r)<0$ (not shown in Figure 1). Comparison with the $\nabla^{2} \zeta(r)$ distribution of an isolated Be atom reveals that large parts of its valence sphere have been lost to the C atoms in the molecules investigated. Hence, a considerable amount of charge seems to be transferred from Be to C in all those compounds. The local energy density $H\left(r_{\mathrm{p}}\right)$

[^2]Table III. Properties of One-Electron Density $\zeta(r)$ and Energy Density $H(r)$ at the Critical Points P (HF/6-31G*)

| molecule | bond | $\zeta_{\mathrm{p}}\left(e / \AA^{\mathbf{3}}\right)$ | $n^{a}$ | $\nabla^{2} \zeta_{p}{ }^{6}\left(e / \AA^{5}\right)$ | $H_{\mathrm{p}}{ }^{\text {c }}$ [hartree $/ \AA^{3}$ ] | $\Delta_{\mathrm{p}}{ }^{\text {d }}$ [\%] |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{CBe}_{2}$, 15 | CBe | 0.666 | 0.9 | 15.2 | -0.15 | 31 |
| $\mathrm{C}_{2} \mathrm{Be}, 4 \mathrm{~S}$ | CC | 2.806 | 2.9 | -34.8 | -3.98 | 0 |
| $\mathrm{C}_{2} \mathrm{Be}_{2}, 6 \mathrm{~S}$ | (C) ${ }_{2} \mathrm{Be}$ | 0.745 |  | 17.7 | -0.13 | 36 |
|  | CC | 2.804 | 2.9 | -30.6 | -5.06 | 27 |
|  | $\mathrm{CBe}^{e}$ | 0.593 | 0.6 | 10.2 | -0.13 | 32 |
|  | BeBe | 0.354 |  | -0.4 | -0.13 | 2 |
| $\mathrm{C}_{2} \mathrm{Be}_{2}, 9 \mathrm{~S}$ | CC | 1.872 | 1.2 | -12.8 | -1.82 | 0 |
|  | CBe | 0.732 | 1.3 | 17.2 | -0.13 | 32 |

${ }^{a}$ Calculated from $n(\mathrm{CC})=\exp \left\{0.94\left(\zeta_{\mathrm{p}}-1.52\right)\right\}$ and $n(\mathrm{CBe})=\exp \left\{5.63\left(\zeta_{\mathrm{p}}-0.69\right)\right\}$. See ref 18 and $20 .{ }^{b}$ See ref 22 . ${ }^{c}$ See ref 20 . ${ }^{d}$ See ref 21 . ${ }^{e}$ Averaged values.


Figure 1. Contourline diagrams of $\nabla^{2} \zeta(r)$. Dashed contour lines indicate molecular regions with charge concentration ( $\nabla^{2}(r)<0$ ). Bond paths are denoted by heavy solid lines, bond critical points by dots: (a) 1 S ; (b) 4 S ; (c) 6 S ; (d) 9 S . Inner shell regions with $\nabla^{2} \zeta(r)<0$ are not shown.
is always close to zero for all CBe bonds considered. This indicates that they are only weakly covalent ${ }^{18 \mathrm{~b}, 23}\left(H\left(r_{\mathrm{p}}\right)<0\right)$ and do possess partial ionic character.

Charge concentration typical of an electron lone pair is found at carbon above and below the molecular plane of IS. As is shown in Figure 2, the IS HOMO is made up essentially of the $\mathrm{p} \pi$ orbital of C , with very little contribution fo the $\mathrm{p} \pi(\mathrm{Be})$ orbitals. Accordingly, we find only moderate $\pi$ character to be present in the $\mathrm{C}-\mathrm{Be}$ bonds of 1 S .

MP2/6-31G* and CASSCF lead to different predictions for the geometry of the lowest lying triplet state (Table I). In view of the high spin contamination of the UHF triplet state, the MP2 relative energies (favoring linear 2T) probably are less reliable than the CASSCF result (which prefers nonlinear 1T). On the
other hand, the CASSCF energy difference between 1 T and 2T may be too small to be conclusive. The linear $\mathrm{Be}-\mathrm{Be}-\mathrm{C}$ arrangement (3T) is the least stable form at all levels.
$\mathrm{C}_{2} \mathrm{Be}$, Two minima each have been found on the singlet and on the triplet $\mathrm{C}_{2} \mathrm{Be}$ potential energy hypersurfaces. Again, the relative energies of the triplets are too low compared to the singlets at the (UHF) SCF level due to the reductions in electron correlation. Both correlated methods agree that the singlet structure 4 S is the $\mathrm{C}_{2} \mathrm{Be}$ global minimum. However, the CASSCF energy differences among $4 \mathrm{~S}, 5 \mathrm{~S}$, and 5 T are not very large and are much smaller than the MP2 differences. Furthermore, optimization of 5 S leads to very different CBe distances with both methods. The $6-31 G^{*}$ value of $1.494 \AA$ corresponds to a CBe double bond, while the $1.652 \AA$ obtained at the CASSCF level indicates a single bond.


Figure 2. HOMO of $\mathrm{CBe}_{2}$ IS, plotted with a contour of 0.1 au .


Figure 3. HOMO of $\mathrm{C}_{2} \mathrm{Be} 4 \mathrm{~S}$, plotted with a contour of 0.1 au .
The coefficients of the leading configurations in the CASSCF optimizations provide an explanation for this discrepancy. The SCF ground-state configuration has a coefficient of 0.74 , but the next important configuration has comparable weight with a coefficient of 0.59 . Both configurations differ in the nature of the highest occupied $\sigma$-type orbital, being the plus and minus combination of the terminal $\sigma$-type lone-pair orbitals


Clearly, reoptimization of the orbitals is very important. Note that the energies and bond distances for the singlet and triplet forms 5 S and 5 T predicted by CASSCF are nearly the same.

One of us considered 4 S as a candidate for a three-membered cyclic structure which might possess a CC triplet bond. ${ }^{24}$ Since that time, two more molecules have been found theoretically with a CC triplet bond in a three-membered ring, i.e., $\mathrm{SiC}_{2}{ }^{25 \mathrm{a}}$ and $\mathrm{MgC}_{2}{ }^{25 \mathrm{~b}}$ There is experimental evidence for a nonlinear geometry of $\mathrm{SiC}_{2}{ }^{26}$ However, the results for $\mathrm{MgC}_{2}$ already are indicative of an ionic rather than a covalent complex. ${ }^{25 b}$ Although covalent bonding is generally stronger for first row than that for second row elements, our analysis of the electron density of 4 S does not reveal any differences for these systems: there are no $\mathrm{C}, \mathrm{Be}$ bond paths corresponding to covalent bonding between these atoms. Instead, we find a path of maximum electron density connecting

[^3]

Figure 4. Second highest occupied MO of $\mathrm{C}_{2} \mathrm{Be} 4 \mathrm{~S}$, plotted with a contour of 0.1 au .


Figure 5. Schematic representation of the valence electrons in $\mathrm{C}_{2} \mathrm{Be}_{2} 7 \mathrm{~T}$.
Be and the $\mathrm{C}, \mathrm{C}$, midpoint (Figure lb ). Hence, 4 S possesses a "T-shaped" rather than a cyclic structure and can be regarded as an ionic complex between $\mathrm{C}_{2}{ }^{2-}$ and $\mathrm{Be}^{2+}$. The CC bond in 4 S is close to a triple bond as revealed by a bond order of $2.9^{18,20}$ (Table III).

Figure 1 b shows that charge is largely depleted from the valence sphere of the Be atom and concentrated both in the CC bonding region and in the regions represented by the back lobes of the $3 \sigma_{\mathrm{g}}$ orbital of $\mathrm{C}_{2}$. This orbital is unoccupied in the ground state of $\mathrm{C}_{2}$ but becomes the HOMO in $\mathrm{C}_{2} \mathrm{Be}$ (Figure 3) due to charge transfer from Be to C . The $\mathrm{p} \pi \mathrm{MO}$ shown in Figure 4 is the second highest occupied MO. Similar to the $\pi \mathrm{MO}$ of $\mathrm{CBe}_{2}$, it is largely made up by carbon $\mathrm{p} \pi$ orbitals indicating that the $2 \pi$ electrons are confined to the $\mathrm{C}, \mathrm{C}$ bond region.
$\mathrm{C}_{2} \mathrm{Be}_{2}$. In contrast to the triatomic molecules, $\mathrm{CBe}_{2}$ and $\mathrm{C}_{2} \mathrm{Be}$, the tetratomic system $\mathrm{C}_{2} \mathrm{Be}_{2}$ is clearly predicted to have a linear triplet global minimum, 7 T , on the potential energy hypersurface. Although we could not perform CASSCF calculations on the $\mathrm{C}_{2} \mathrm{Be}_{2}$ isomers, the $3-21 \mathrm{G}$ and $6-31 \mathrm{G}^{*}$ single determinant relative energies are quite unambiguous and are consistent with regard to the lowest-energy form. Inclusion of correlation energy at the MP2/6-31G* level leads to an increase in the stability difference to more than $80 \mathrm{kcal} / \mathrm{mol}$ relative to the second lowest isomer, the singlet 6 S . Because of the large energy difference, it seems certain that 7 T represents the most stable $\mathrm{C}_{2} \mathrm{Be}_{2}$ isomer. The high stability of 7 T is due to the favorable acetylene-like structure with a strong CC triple bond and the two unpaired electrons at the beryllium atoms in the $\sigma$-orbitals pointing away from the carbon atoms, as shown in Figure 5. The electronic structure of 5T, which can be represented as $\uparrow \mathrm{C} \equiv \mathrm{C}-\mathrm{Be} \uparrow$, is closely related.

The remaining $\mathrm{C}_{2} \mathrm{Be}_{2}$ forms are too high in energy to expect experimental verification. However, some of the structural features are quite interesting from a theoretical point of view, especially in comparison with other molecules. Epiotis predicted ${ }^{27}$ on the basis of his MOVB model ${ }^{28,29}$ that the relative energy difference

[^4]favoring the rhomboidal isomer 9S over the linear form 7S should be larger than the difference between the analogous structures of $\mathrm{C}_{4}$. At the same level of theory as employed here (MP2/6$31 \mathrm{G}^{* *} / / 6-31 \mathrm{G}^{*}$ ), the $\mathrm{C}_{4}$ linear singlet is only $14.6 \mathrm{kcal} / \mathrm{mol}$ higher in energy than the rhomboidal form. ${ }^{30}$ This energy difference is clearly much smaller than that of the $\mathrm{C}_{2} \mathrm{Be}_{2}$ singlets, in accord with Epiotis's conclusion.

The geometry of 6 S is interesting since symmetry reduction occurs from $C_{2 i}$ to $C_{s}$ symmetry due to second-order Jahn-Teller distortion. The electron density analysis for the singlet 6 S shows that there is again a considerable charge transfer from Be to C . The CBe bonds are weak, while the CC bond possesses a bond order close to 3 ( $n=2.9$, Table III). For the bicyclic isomer 9 S , however, the CBe bonds are relatively strong ( $n=1.3$ ), while the CC bond is surprisingly weak ( $n=1.2$ ). The $2 \pi$ electrons of both 6 S and 9 S are largely confined to the CC bond.

## IV. Discussion

The bonding in these molecules cannot be discerned adequately by conventional criteria. Geometrical parameters (distances and angles) are clearly not sufficient to distinguish between what might be termed T-shaped or cyclic bonding. Dewar and Ford ${ }^{31}$ differentiated in the case of nonlinear three heavy atom systems between cyclic structures and $\pi$-complexes utilizing MO theory. Clearly, a correct representation of the electronic structure is necessary to describe the BeC compounds.

In view of the structural peculiarities of the molecules investigated one may ask which model is best suited to give an understanding of CBe bonding. For example, Walsh rules ${ }^{19}$ may be used. They correctly predict a bent geometry for the eight-valence-electron system $\mathrm{CBe}_{2}$ but fail in the case of the ten-electron system $\mathrm{C}_{2} \mathrm{Be}$, where a linear structure is expected rather than the nonlinear form we have found. This failure is probably due to the fact that Walsh rules have been developed on the basis of covalent bonding while CBe interactions have considerable ionic character.

The more subtle bonding features, of the nonlinear geometries in particular, can be understood by considering donor-acceptor interactions. ${ }^{18,31}$ The more electropositive Be tends to donate its valence electrons to carbon. This electron donation, however, depends on the nature and the symmetry of the carbon acceptor orbitals and the degree of overlap. As shown in generalized form at the top of Figure 6, two orbitals, designated $b_{2}$ and $a_{1}$, are present in the fragments, $X$ and $X_{2}(X=B e$ or $C)$, which will interact in $C_{2 v}$ symmetry. These combinations, shown for $\mathrm{C}_{2} \mathrm{Be}$ at the left bottom of Figure 6, involving charge transfer from the $\mathrm{a}_{1}(\mathrm{Be})$ orbital to the $\mathrm{a}_{1}$ orbital of $\mathrm{C}_{2}$, are responsible for the T-shaped electronic structure of 4 S and for a CC bond order close to 3 . A cyclic electronic structure would result if significant back-donation to Be were to occur from an occupied $\mathrm{b}_{2}(\mathrm{CC})$ orbital or if charge transfer from $B e$ to $C$ were to take place via the $\mathrm{B}_{2}$ orbital because of partial or full occupation of the bonding $a_{1}\left(C_{2}\right)$ orbital.

The bonding feature of 4 S may be compared to Dewar and Ford's (DF) concept of olefinic $\pi$-complexes vs. ring structures. ${ }^{31}$ In their definition, a $\pi$-complex is charcterized by a $\pi$-donor bond of the CC unit to the apical atom without significant back donation. A true ring structure is found when back-coordination becomes important which is the case for less electronegative atoms or groups. ${ }^{31} 4 \mathrm{~S}$ may serve as an example where in terms of DF only back-donation takes place resulting in an electronic structure which they may also call a $\pi$-complex.

Can true cyclic structures with $\mathrm{C}-\mathrm{Be}$ bonding be formed at all? The answer is yes. For example, in the case of 9 S (Figure 6,

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Figure 6. Donor and acceptor orbitals of $\mathrm{C}(\mathrm{Be})$ and $\mathrm{C}_{2}\left(\mathrm{Be}_{2}\right)$ with $\mathrm{a}_{1}$ or $\mathrm{b}_{2}$ symmetry.
bottom right) one electron can be donated from each Be to $\mathrm{C}_{2}$ via the $a_{1}$ orbital and one each via the $b_{2}$ orbital. As a consequence, the relative high electron concentration in the region of the $b_{2}$ orbitals indicative of relatively strong CBe bonds results. This alternative mode of donation from Be gives rise to the weak CC bond in 9S (see Table III and Figure 1d).

The electronic structure of 1 S contrasts with that of 4 S . Consider the diagram at the bottom left of Figure 6 but with C in place of Be and $\mathrm{Be}_{2}$ in place of $\mathrm{C}_{2}$. In $\mathrm{CBe}_{2}(1 \mathrm{~S})$, charge is donated from the bonding $\mathrm{a}_{1}$ orbital of $\mathrm{Be}_{2}$ to a vacant carbon p-orbital ( $\mathrm{a}_{1}$ ). This weakens the bonding Be-Be interaction and would lead to a structure similar to a T -form. ${ }^{18 \mathrm{c}}$ However, back-donation from the filled carbon $b_{2}$ orbital into the $\mathrm{Be}_{2}$ fragment orbital of the same symmetry results in $\mathrm{C}-\mathrm{Be}$ bonding but in $\mathrm{Be}-\mathrm{Be}$ antibonding. This participation of the $\mathrm{b}_{2}(\mathrm{C})$ orbital in CBe bonding is seen in Figure 1a. Charge concentrates in the area of the $b_{2}$ orbital and the bond paths curve outwardly; close to the C nucleus they almost follow the direction of the $\mathrm{b}_{2}$ orbital. The different electronic structure of $\mathrm{C}_{2} \mathrm{Be}(4 \mathrm{~S}$, Figure 1 b ) is due to the extra pair of electrons involved in CC bonding and the greater electronegativity of carbon relative to beryllium.

The bonding situation in 6 S is similar to that in 1 S . If the interacting $\mathrm{Be}_{2}$ and $\mathrm{C}_{2}$ fragments are arranged in $C_{2 v}$ symmetry to allow maximum overlap between their $\mathrm{b}_{2}$ orbitals, charge transfer from $\mathrm{Be}_{2}$ to $\mathrm{C}_{2}$ will significantly reduce the CC bond strength and, therefore, will be unfavorable energetically. Stabilization, however, can be achieved by a distortion of the rectangular $C_{2 v}$ arrangement to the lower $C_{s}$ symmetry observed for 6 S . The consequent mixing of the $\mathrm{a}_{1}$ and $\mathrm{b}_{2}$ MOs allows direct charge transfer from the $\mathrm{Be}_{2}$ fragment into the " $\mathrm{a}_{1}$ " MO of $\mathrm{C}_{2}{ }^{36}$ Thus, the CC bond order is enhanced from 2 nearly to 3 . This is in line with the density (Table III) and concentration pattern of electrons found for 6S (Figure 1c).

On the basis of the simple donor-acceptor moc'el outlined above and the characteristic charge density (concentration) patterns shown in Figure 1 it is now possible to make structural predictions with regard to other compounds. For example, $\mathrm{C}_{2}(\mathrm{BeH})_{2}$ in $D_{2 h}$ symmetry should possess a double-T electronic structure rather than the bicyclic structure of 9 S . Be bound to either $\mathrm{C}_{2} \mathrm{H}_{2}, \mathrm{C}_{2} \mathrm{H}_{4}$, $\mathrm{N}_{2}$, or $\mathrm{O}_{2}$ in $C_{2 v}$ symmetry will lead to ring-shaped rather than T-shaped electronic structures since charge transfer has to occur bia $b_{2}$ orbitals. Work is in progress to test these predictions ${ }^{33}$ (Chart I).

Both 1 S and 4 S might be considered as $2 \pi$ Hückel aromatic compounds on the basis of a simple electron count. However, $\zeta(r)$ analysis clearly shows that the $2 \pi$ electrons of 1 S and 4 S are

Chart I

confined largely to the carbon regions. Since this also applies to 6 S and 9 S , carbon bonded to Be is a very weak $\pi$-donor. Thus, the basic electronic requirement for aromaticity, namely $\pi$-electron delocalization, is not fulfilled. As a consequence, we do not consider any of these compounds to be aromatic. ${ }^{34}$

To assess the thermodynamic stabilities of the global minima $1 \mathrm{~S}, 4 \mathrm{~S}$, and 7 T in regard to fragmentation processes, we calculated the heats of reaction for reactions $1-6$ at the MP2/6-31G*//6$31 \mathrm{G}^{*}$ level ${ }^{32}$

$$
\begin{align*}
& 1 \mathrm{~S} \rightarrow \mathrm{CBe}+\mathrm{Be}+68.0 \mathrm{kcal} / \mathrm{mol}  \tag{1}\\
& 1 \mathrm{~S} \rightarrow \mathrm{C}+2 \mathrm{Be}+120.4 \mathrm{kcal} / \mathrm{mol}  \tag{2}\\
& 1 \mathrm{~S} \rightarrow \mathrm{C}+\mathrm{Be}+119.8 \mathrm{kcal} / \mathrm{mol}  \tag{3}\\
& 4 \mathrm{~S} \rightarrow \mathrm{C}_{2}+\mathrm{Be}+111.6 \mathrm{kcal} / \mathrm{mol}  \tag{4}\\
& 4 \mathrm{~S} \rightarrow \mathrm{CBe}+\mathrm{C}+203.3 \mathrm{kcal} / \mathrm{mol}  \tag{5}\\
& 7 \mathrm{~T} \rightarrow 4 \mathrm{~S}+\mathrm{Be}+103.7 \mathrm{kcal} / \mathrm{mol} \tag{6}
\end{align*}
$$

[^6]The large positive values for all of the reactions $1-6$ show that bonding in $\mathrm{IS}, 4 \mathrm{~S}$, and 7 T is quite strong and that all three compounds should be very stable in the gas phase.

## V. Conclusions

(1) The global minima of the potential energy hypersurfaces of $\mathrm{CBe}_{2}$ and $\mathrm{C}_{2} \mathrm{Be}$ correspond to the singlet nonlinear $C_{2 i}$ geometries 1 S and 4 S , respectively. However, CASSCF calculations on $\mathrm{C}_{2} \mathrm{Be}$ indicate the linear $\bullet \mathrm{C} \equiv \mathrm{C}-\mathrm{Be} \bullet$ geometries, 5 S and 5 T , to be quite low in energy. The most stable $\mathrm{C}_{2} \mathrm{Be}_{2}$ geometry is the linear triplet $7 \mathrm{~T}, \uparrow \mathrm{Be}-\mathrm{C} \equiv \mathrm{C}-\mathrm{Be} \uparrow$. All other linear and cyclic forms are much higher in energy.
(2) Charge transfer from Be to C is the dominating force in all compounds considered. As a consequence, the CBe bonds in these molecules are only weakly covalent.
(3) Charge transfer interactions can be described by a simple donor-acceptor MO model that allows predictions with regard to CBe bonding in the nonlinear geometries. Depending on the mode of charge transfer (either via $a_{1}$ or $b_{2}$ orbitals) one can expect T-shaped (4S), bent (1S), or cyclic structures ( 6 S and 9 S ) (Figure 1).
(4) Bonding and structural features are reflected by $\zeta(r)$ and $\nabla^{2} \zeta(r)$. Participation of $b_{2}$-orbitals in bonding leads to a concentration pattern (Figure 1 d ) rather different from that due to charge transfer via $a_{1}$-orbitals (Figure $1 b$ ).
(5) $\pi$-delocalization in these cyclic CBe compounds is small. None of these can be called aromatic, which is probably to be expected for other CBe compounds.

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Registry No. $\mathrm{CBe}_{2}$, 506-66-1; $\mathrm{C}_{2} \mathrm{Be}, 94740-29-1 ; \mathrm{C}_{2} \mathrm{Be}_{2}$, 103619-64-3.

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[^0]:    ${ }^{+}$Technische Universität Berlin.
    \# Universität Köln.
    ${ }^{8}$ Universität Erlangen-Nürnberg.

[^1]:    (19) (a) Walsh, A. D. J. Chem. Soc. 1953, 2260, 2266, 2288, 2296, 2301, 2306, 2318, 2321, 2325, 2330. (b) Gimarc, B. M. Molecular Structure and Bonding; Academic Press: New York 1979.

[^2]:    (20) The bond critical point $P$ corresponds to the minimum of $\zeta(r)$ along the path of maximum electron density connecting two atomic nuclei A and B. (Point $P$ is a saddle point of $\zeta(r)$ in three dimensions). According to Cremer and Kraka ${ }^{18}$ a covalent bond between two atoms exists if (i) a bond critical point is found between A and B (necessary condition) and (ii) the local energy density $H\left(r_{\mathrm{p}}\right)$ is lower than zero (sufficient condition). Utilizing calculated values $\rho_{\mathrm{p}}$, a bond order $n$ can be defined according to $n(A, B)=\exp$ ( $a\left[\zeta_{p}(A, B)-\mathrm{b}\right]$ ). At the HF/6-31G* level, the following constants have been used $a(\mathrm{CC})=0.94, b(\mathrm{CC})=1.52\left(e / \AA^{3}\right)^{18 b}, a(\mathrm{CBe})=5.63 ; b(\mathrm{CBe})=0.69$ (e/ $\AA^{3}$ ). The latter have been evaluated by using $\mathrm{CH}_{3} \mathrm{BeH}$ and $\mathrm{CH}_{2} \mathrm{Be}$ as reference compounds.
    (21) The position of the point $P$ is determined by the parameter $\Delta_{p}$ which is zero for $P$ at the midpoint of the bond and larger than zero for a shift of $\mathbf{P}$ in the direction of the electropositive atom. The value of $\Delta_{\mathrm{p}}$ is the larger the larger the charge transfer and the more polar the bond is. If bonds between atoms of different rows of the periodic system are considered, the different number of inner shells has to be taken into account.
    (22) In general, the Laplacian of any scalar field is negative, where the scalar field concentrates while it is positive, where the scalar fields expands. For more information, see: Bader, R. F. W.; Essen, H. J. Chem. Phys. 1984, 80, 1943 and ref 18 b and 18 c .
    (23) The term "structure" is is used here in the topological sense as defined by Bader, R. F. W.; Tal, Y.; Anderson, S. G.; Nguyen-Dang, T. T. Israel. J. Chem. 1980, 19, 8.

[^3]:    (24) Frenking, G. Chem. Phys. Lett. 1984, 111, 529.
    (25) (a) Grev, R. S. Schaefer, H. F.; III. J. Chem. Phys. 1984, 80, 3552
    (b) Green, S.; Chem. Phys. Lett. 1984, 112, 29.
    (26) Michalopoulos, D. L.; Geusic, M. W.; Langridge-Smith, P. R. R.; Smalley, R. E. J. Chem. Phys. 1984, 80, 3556.

[^4]:    (27) Epiotis, N. D. J. Am. Chem. Soc. 1984, 106, 3170.

[^5]:    (28) Epiotis, N. D. Unified Valence Bond Theory of Electronic Structure; Lecture Notes in Chemistry; Springer Verlag: Berlin, 1982; Vol. 29. (b) Epiotis, N. D. "Unified Valence Bond Theory of Electronic StructureApplications"; Lecture Notes in Chemistry; Springer Verlag: Berlin, 1983; Vol. 34.
    (29) Epiotis, N. D. Pure Appl. Chem. 1983, 55, 229.
    (30) Whiteside, R. A.; Krishnan, R.; DeFrees, D. J.; Pople, J. A.; Schleyer, P. v. R. Chem. Phys. Lett. 1981, 78, 538.
    (31) Dewar, M. J. S.; Ford, G. P. J. Am. Chem. Soc. 1979, 101, 783.

[^6]:    (32) The following total energies (au) have been taken at the MP2/6 31G//6-31G* level from ref 35: $\mathrm{Be}\left({ }^{1} \mathrm{~S}\right)-14.5933 ; \mathrm{Be}_{2}\left({ }^{( } \Sigma_{\mathrm{g}}{ }^{+}\right)-29.1874 ; \mathrm{C}\left({ }^{3} \mathrm{P}\right)$ -37.7330; $\mathrm{C}_{2}\left({ }^{1} \Sigma_{\mathrm{g}}{ }^{+}\right)-75.6955$. For $\mathrm{CBe}\left({ }^{3} \Sigma^{-}\right)$the MP2/6-31G* energy was calculated by using the $6-31 \mathrm{G}^{*}$ bond distance of $1.661 \AA$ taken from ref 35 : -52.4097 . Note that some of the reactions are spin forbidden, the spin allowed processes are thermodynamically even less favorable.
    (33) Cremer, D.; Gauss, J.; Frenking, G.; Koch, W.; Schleyer, P. v. R., to be published.
    (34) A similar conclusion has been drawn for $\mathrm{C}_{2} \mathrm{Be}$ on the basis of semiempirical calculations: Gropinathan, M. S.; Jug, K. Theor. Chim. Acta 1983, 63,511.
    (35) Whiteside, R. A., Frisch, M. J., Pople, J. A., Eds.; The CarnegieMellon Quantum Chemistry Archive, 3rd. ed., Carnegie-Mellon University: Pittsburgh, 1983.

[^7]:    (36) The distribution $\zeta(r)$ in the $\mathrm{Be}, \mathrm{Be}$ internuclear region of 6 S is rather flat. For example, the value of $\zeta(r)$ at the saddle point between the Be atoms is only slightly large than at the ring critical point. Therefore, we cannot exclude that an acyclic structure similar to $1 \mathbf{S}$ is found for 6 S at higher levels of theory.

